

# On the generation of collision-probability matrices with Serpent 2

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# Overview

- ▶ Motivation and overview of the CP method.
- ▶ Generation of collision probability matrices in Serpent 2.
- ▶ CP matrix structure – examples.
- ▶ Application of CP matrices to simplified problems.
- ▶ Future prospects.

Motivation

# Motivation

- ▶ To develop a(nother) low-order neutronics solver in the Kraken framework.
- ▶ Exploit the unique capabilities of MC techniques for tracking in complex geometries.
- ▶ Relax some of the assumptions of the collision-probability method:
  - Flat source approximation
  - Isotropic neutron sources
  - Isotropic/cosine angular currents
- ▶ Combine the CP-method with homogenized XS data generated by Serpent → drastically reduce the number of energy groups.
- ▶ Decompose the problem into nodes coupled by boundary currents. Solve one CP problem inside every node.
- ▶ Explore the application of 3-D CP-methods to, e.g., ex-core radiation transport.

# An overview of the CP method

# The Collision Probability method

- ▶ Partition  $V = \{V_1, V_2, \dots, V_i, \dots, V_N\}$ ; and  $\Gamma$
- ▶ Evaluate collision probability matrices:

$P$  : *first-flight* collision probabilities

$E$  : *escape* collision probabilities

$G$  : cell *opacity*

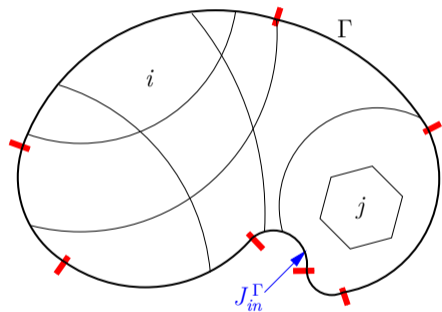
$T$  : surface segment *transmission* (or *transparency*)

- ▶ Solve the systems:

$$\Sigma_{t,g}^i \Phi_g^i V_i = \sum_{\forall j} [P_{j \rightarrow i} Q_{t,g}^g V_j] + \sum_{\forall s} [G_{s \rightarrow i} J_{in}^{g,s} A_s]$$

$$J_{out}^{g,s} A_s = \sum_{\forall j} [E_{j \rightarrow s} Q_{t,g}^g V_j] + \sum_{\forall s'} [T_{s' \rightarrow s} J_{in}^{g,s'} A_{s'}]$$

- ▶  $Q_{t,g}^g = Q_{ext,g}^g + Q_{fis,g}^g + Q_{down,g}^g + \sum_{s,g \rightarrow g}^i \Phi_g^i + Q_{up,g}^g$
- ▶ Can replace  $\Phi_g^i V_i$  and  $J_{in}^{g,s} A_s$  by volume- and surface-integrated values



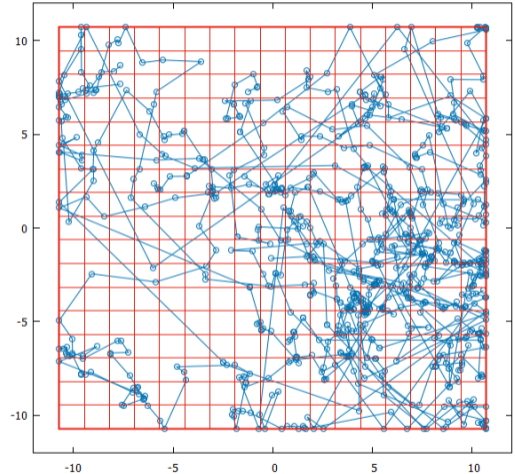
# Implementation in Serpent

# Implementation in Serpent

- ▶ Implemented in Serpent version 2.1.29.
- ▶ Scores various arrays upon source, (physical) collision and outer boundary crossing events.
- ▶ Enforces

`DATA_STOP_AT_BOUNDARY = YES`

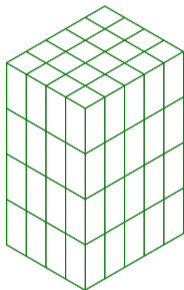
- ▶ Only works with *reflective* boundary conditions.
- ▶ For depletion problems, generates CP matrices (P, E, G, and T) per burnup step.
- ▶ Data output in Octave/MatLab format.
- ▶ Face numbering for efficient coupling in second step (outside solver).
- ▶ About geometry...



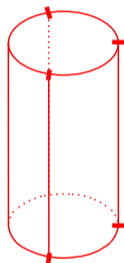


## CP – geometry

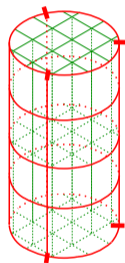
- ▶ Combines a CP mesh ( $V$ ) and a container box ( $\Gamma$ ).
- ▶ CP mesh used for scoring all P elements, domain of  $E$ , image of  $G$ .
- ▶ “Extended” container box for scoring all T elements, domain of  $G$ , image of  $E$ .
- ▶ Axial discretization from the CP mesh.
- ▶ Radial *face* discretization from container box.
- ▶ Top and bottom face discretization given by the CP mesh.



CP  
mesh



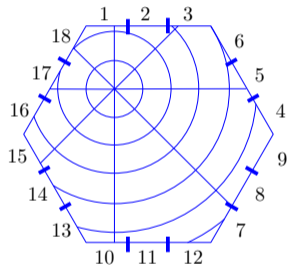
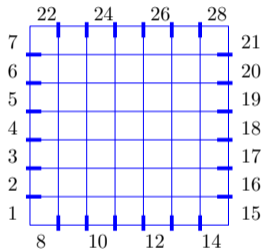
Container  
box



CP  
geometry

## Radial segment numbering

- ▶ Per axial level, the discretization follows the container box  
**SEGFACE** value, **not** the one of the CP mesh.
- ▶ Face sweeping order is given by DFPos().
- ▶ Sweeping order per mesh is related to Cartesian coordinates.
- ▶ Top and bottom faces (not shown) follow the –shifted– numbering of the CP meshes, as in standard mesh detectors.



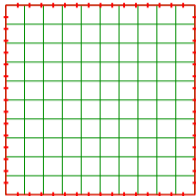
## cpmat cards

```
cpmat  NAME  SURF  FACESEG
      [ PART ]
      [ dx XMIN XMAX NX ]
      [ dy YMIN YMAX NY ]
      [ dz ZMIN ZMAX NZ ]
      [ dn  -1  MIN1 MAX1 N1 MIN2 MAX2 N2 MIN3 MAX3 N3 ]
      [ dh TYPE X0 Y0 PITCH N1 N2 ZMIN ZMAX NZ ]
      [ 2d ]
```

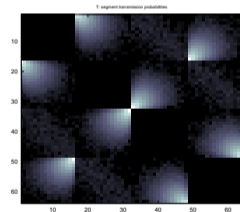
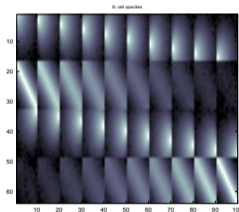
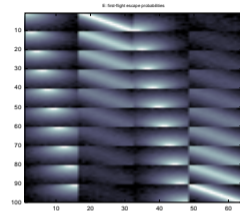
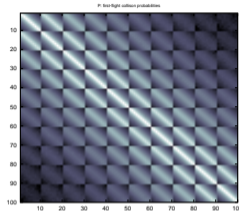
- ▶ Do not use periodic BCs.
- ▶ Group structure is taken from set nfg card.
- ▶ Container box (SURF) needs not be a part of the geometry, but consistent with the 2d radial flag.
- ▶ Good practice: CP mesh fully contained within the (whole) problem geometry.

# CP matrix structure – examples

# Example 1 – 2-D: all in order



P, E ↗  
G, T →



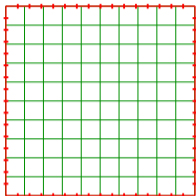
cpmat cards in Serpent →



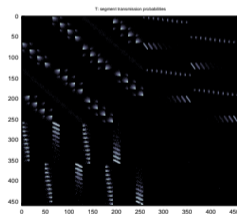
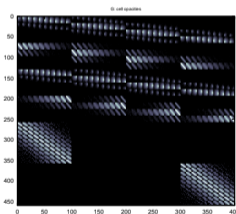
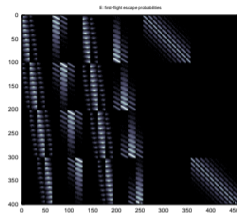
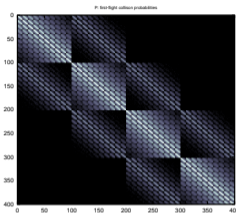
```
cpmat ex_1 115          16
      dx -10.71    10.71  10
      dy -10.71    10.71  10
      dz  0.0      365.76  1
      2d  yes

surf 115  rect  -10.71  10.71  -10.71  10.71
```

## Example 2 – 3-D: all in order



P, E ↗  
G, T →



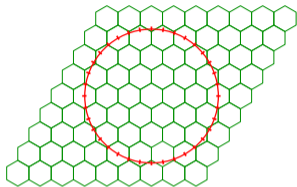
cpmat cards in Serpent →



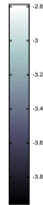
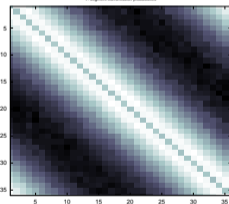
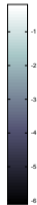
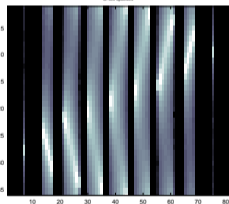
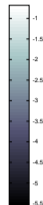
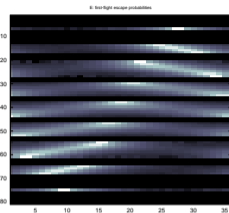
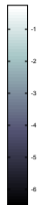
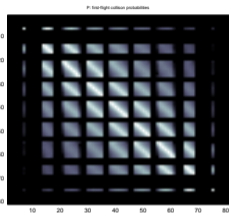
```
cpmat ex_2 116 16
dx -10.71 10.71 10
dy -10.71 10.71 10
dz 0.0 365.76 4
2d no

surf 116 cuboid -10.71 10.71 -10.71 10.71 0.0 365.76
```

## Example 3 – 2-D: cylindrical container box



P, E ↗  
G, T →



cpmat cards in Serpent →

```
cpmat ex_3 106 36
dh 2 0.0 0.0 2.0 9 9 0.0 365.76 1
2d yes

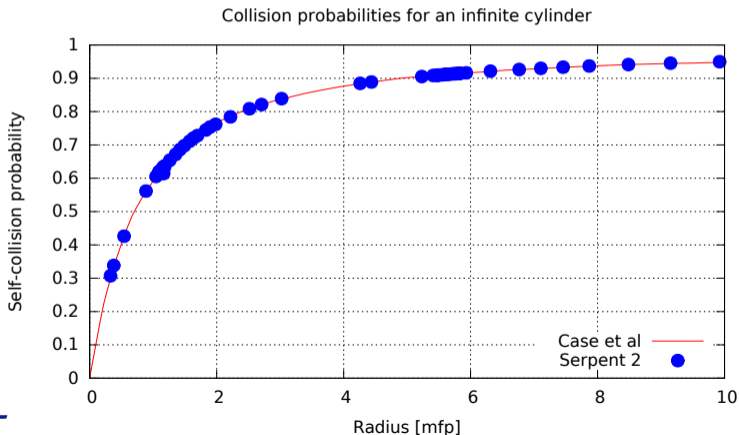
surf 106 cyl 0.0 0.0 6.000
```

Verification case: infinite cylinder



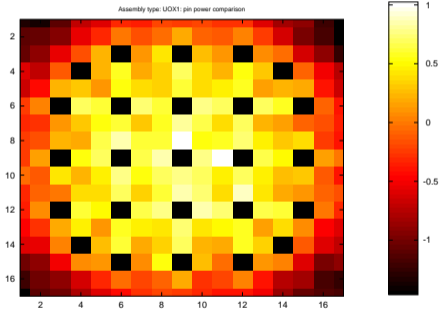
# Infinite cylinder

- ▶ Infinite cylinder with uniform, isotropic source with 1 MeV neutrons.
- ▶ Serpent input for a water region. Data generated in 40 energy groups.



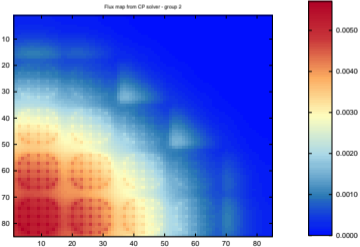
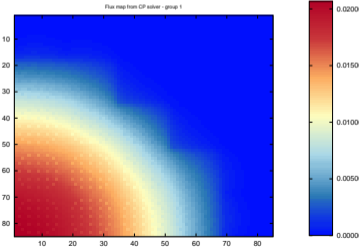
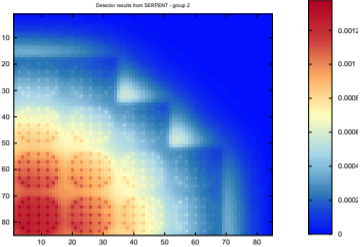
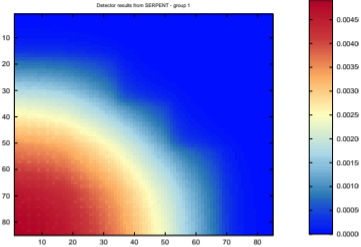
Example cases in Cartesian geometry

# UOX1 PWR assembly from KAERI benchmark 1B

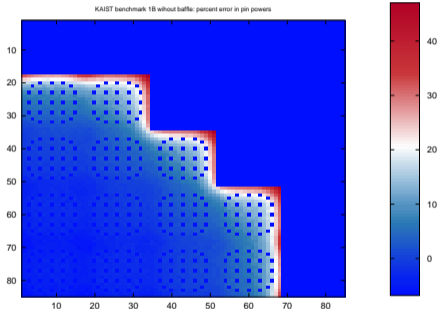


- ▶ XS and CP data generated in two energy groups for 2 pin types:
  - guide tubes
  - UOX 2.2 %
- ▶  $\Delta\rho = 3$  pcm
- ▶ Maximum pin power difference against Serpent: 1.5 %

# Simplified version of the KAERI benchmark 1B problem: fluxes



# Simplified KAERI benchmark 1B problem: general



- ▶ Much to be improved:
  - $\Delta_\rho = 1250$  pcm
  - Maximum difference in pin-powers with Serpent: 47 %
- ▶ Other cases suggest that the problem is in the reflectors
- ▶ Possible solutions:
  - Model reflector XS data with spatial variations
  - Increase energy resolution
  - Replace reflectors by segment-wise albedos (available from CP generation routines)
  - Application of equivalence through SPH factors

Ongoing and future work

## Ongoing and future work

- ▶ Support for binary print of CP data in Serpent.
- ▶ Development of a comprehensive, parallel, CP-based solver for fixed/adjoint source and eigenvalue calculations.
- ▶ Implementation of CP matrix perturbation models for SPH factor computations.
- ▶ Development of Coarse Mesh Collision Probability (CMCP) acceleration scheme.
- ▶ Testing on shielding problems.



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